

EXAMEN 2012

I) 2) a) $R_L = \sqrt{\frac{M_L \cdot k}{G_L}} = \sqrt{\frac{5,98 \cdot 10^{24} \cdot 6,67 \cdot 10^{-11}}{81 \cdot 1,6}} \text{ m} = 1,754 \cdot 10^6 \text{ m}$
 $\rightarrow d_L = 3508 \text{ Km}$

b) $\gamma = \sqrt[3]{G_L \left(\frac{T \cdot R_L}{2\pi}\right)^2} - R_L = \sqrt[3]{1,6 \cdot \left(\frac{7150 \cdot 1,754 \cdot 10^6}{2\pi}\right)^2} - 1,754 \cdot 10^6 = 10^5 \text{ m}$
 $= 100 \text{ Km}$

II) 2) a) $T_0 = 2\pi \sqrt{\frac{m}{k_1}} = 0,567 \text{ s}$; $\omega_0 = \frac{2\pi}{T_0} = 11,08 \frac{\text{rad}}{\text{s}}$

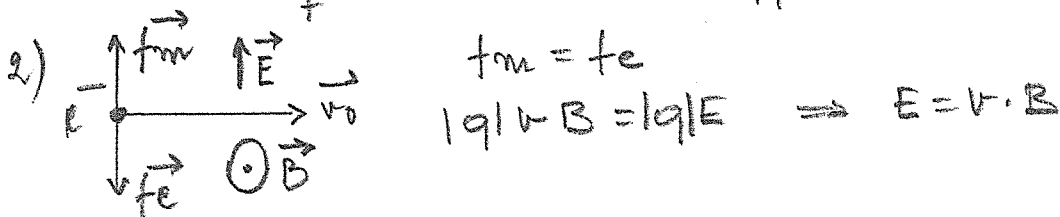
b) $E = \frac{kx^2}{2} = \frac{12,3 \cdot 0,03^2}{2} \text{ J} = 0,00554 \text{ J}$

$x = 0,03 \cos 11,08t \Rightarrow x(0,5 \text{ s}) = 0,022 \text{ m}$

$v = -0,03 \cdot 11,08 \sin 11,08t \Rightarrow v(0,5 \text{ s}) = 0,225 \frac{\text{m}}{\text{s}}$

$a = -0,03 \cdot 11,08^2 \cos 11,08t \Rightarrow a(0,5 \text{ s}) = -2,71 \frac{\text{m}}{\text{s}^2}$

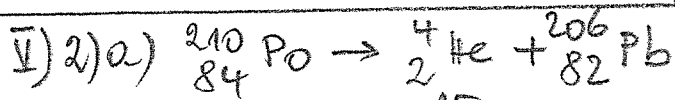
III) 1) $n = 2fL \sqrt{\frac{\mu}{F}}$ et $n' = 2 \cdot 4f \cdot L \sqrt{\frac{\mu}{4F}} = 2n \Rightarrow n$ double



IV) 3) a) $0 = -\frac{gt^2}{2} + v_0 \sin \alpha \cdot t + h \Rightarrow 4,905t^2 - 2,89t - 6 = 0$
 $\Rightarrow t = \frac{2,89 \pm \sqrt{2,89^2 + 4 \cdot 4,905 \cdot 6}}{2 \cdot 4,905} \Rightarrow t = 1,44 \text{ s}$

b) $v = \sqrt{v_x^2 + v_y^2}$ avec $v_x = v_0 \cos \alpha = 3,45 \frac{\text{m}}{\text{s}}$
 $v_y = -gt + v_0 \sin \alpha = -9,81 \cdot 1,44 + 4,5 \sin 40^\circ = -11,23 \frac{\text{m}}{\text{s}}$

$v = 11,75 \frac{\text{m}}{\text{s}}$ et $\tan \beta = \frac{v_y}{v_x} = -3,25 \Rightarrow |\beta| = 73^\circ$



b) $A_0 = \frac{1,88 \cdot 10^{15}}{360} = 5,22 \cdot 10^{12} \text{ Bq}$

c) $N_0 = \frac{A_0}{\lambda} = \frac{5,22 \cdot 10^{12} \cdot 138 \cdot 86400}{\ln 2} = 8,98 \cdot 10^{19} \text{ noyaux}$

d) $N_0 = \frac{m_0}{M} \cdot N_A \Rightarrow m_0 = \frac{N_0 M}{N_A} = \frac{8,98 \cdot 10^{19} \cdot 210}{6,022 \cdot 10^{23}} \text{ g} = 0,031 \text{ g}$

e) $8000 = 5,22 \cdot 10^{12} \cdot e^{-\lambda t} \Rightarrow -\lambda t = \ln \frac{8000}{5,22 \cdot 10^{12}} = -20,3$

$\Rightarrow t = \frac{20,3}{\lambda} = \frac{20,3 \cdot T_{1/2}}{\ln 2} = 4041 \text{ jours} \approx 11 \text{ ans}$